

CCC '18 S4 - Balanced Trees

Time Limit: 2.0s Memory Limit: 256M

Canadian Computing Competition: 2018 Stage 1, Senior #4

Trees have many fascinating properties. While this is primarily true for trees in nature, the concept of trees in math and computer science is also interesting. A particular kind of tree, a *perfectly balanced tree*, is defined as follows.

Every perfectly balanced tree has a positive integer *weight*. A perfectly balanced tree of weight 1 always consists of a single node. Otherwise, if the weight of a perfectly balanced tree is w and $w \geq 2$, then the tree consists of a root node with branches to k subtrees, such that $2 \leq k \leq w$. In this case, all k subtrees must be completely identical, and be perfectly balanced themselves.

In particular, all k subtrees must have the same weight. This common weight must be the maximum integer value such that the sum of the weights of all k subtrees does not exceed w , the weight of the overall tree. For example, if a perfectly balanced tree of weight 8 has 3 subtrees, then each subtree would have weight 2 , since $2 + 2 + 2 = 6 \leq 8$.

Given N , find the number of perfectly balanced trees with weight N .

Input Specification

The input will be a single line containing the integer N ($1 \leq N \leq 10^9$).

For 5 of the 15 marks available, $N \leq 1\,000$.

For an additional 2 of the 15 marks available, $N \leq 50\,000$.

For an additional 2 of the 15 marks available, $N \leq 10^6$.

Output Specification

Output a single integer, the number of perfectly balanced trees with weight N .

Sample Input 1

4

Sample Output 1

3

Explanation for Sample Output 1

One tree has a root with four subtrees of weight 1; a second tree has a root with two subtrees of weight 2; the third tree has a root with three subtrees of weight 1.

Sample Input 2

10

Sample Output 2

13